

CS 188: Artificial Intelligence

Lecture 19: Decision Diagrams

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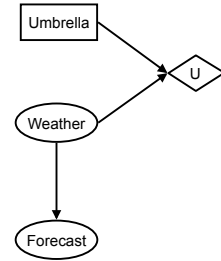
Many slides over this course adapted from Dan Klein, Stuart Russell, Andrew Moore

Decision Networks

- MEU: choose the action which maximizes the expected utility given the evidence
- Can directly operationalize this with decision networks
 - Bayes nets with nodes for utility and actions
 - Lets us calculate the expected utility for each action

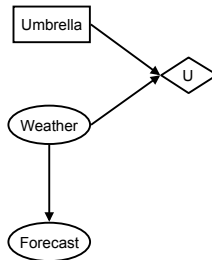
New node types:

- Chance nodes (just like BNs)
- Actions (rectangles, cannot have parents, act as observed evidence)
- Utility node (diamond, depends on action and chance nodes)



Decision Networks

- Action selection:**
 - Instantiate all evidence
 - Set action node(s) each possible way
 - Calculate posterior for all parents of utility node, given the evidence
 - Calculate expected utility for each action
 - Choose maximizing action



Example: Decision Networks

Umbrella = leave

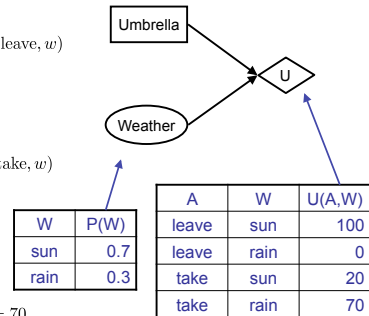
$$EU(\text{leave}) = \sum_w P(w)U(\text{leave}, w) = 0.7 \cdot 100 + 0.3 \cdot 0 = 70$$

Umbrella = take

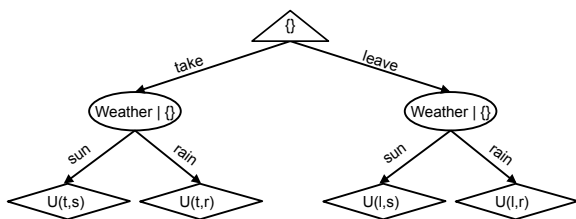
$$EU(\text{take}) = \sum_w P(w)U(\text{take}, w) = 0.7 \cdot 20 + 0.3 \cdot 70 = 35$$

Optimal decision = leave

$$MEU(\emptyset) = \max_a EU(a) = 70$$



Decisions as Outcome Trees



- Almost exactly like expectimax / MDPs
- What's changed?

Example: Decision Networks

Umbrella = leave

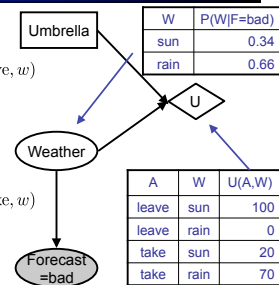
$$EU(\text{leave}|\text{bad}) = \sum_w P(w|\text{bad})U(\text{leave}, w) = 0.34 \cdot 100 + 0.66 \cdot 0 = 34$$

Umbrella = take

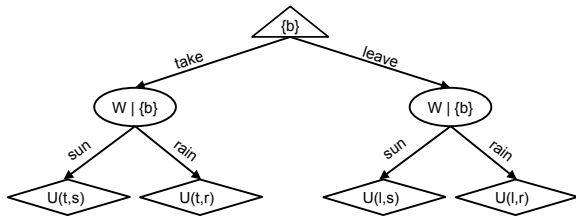
$$EU(\text{take}|\text{bad}) = \sum_w P(w|\text{bad})U(\text{take}, w) = 0.34 \cdot 20 + 0.66 \cdot 70 = 53$$

Optimal decision = take

$$MEU(F = \text{bad}) = \max_a EU(a|\text{bad}) = 53$$



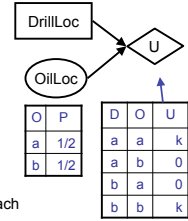
Decisions as Outcome Trees



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Value of Information

- Idea: compute value of acquiring evidence
 - Can be done directly from decision network
- Example: buying oil drilling rights
 - Two blocks A and B, exactly one has oil, worth k
 - You can drill in one location
 - Prior probabilities 0.5 each, & mutually exclusive
 - Drilling in either A or B has $EU = k/2$, $MEU = k/2$
- Question: what's the value of information of O?
 - Value of knowing which of A or B has oil
 - Value is expected gain in MEU from new info
 - Survey may say "oil in a" or "oil in b," prob 0.5 each
 - If we know OilLoc, MEU is k (either way)
 - Gain in MEU from knowing OilLoc?
 - $VPI(OilLoc) = k/2$
 - Fair price of information: $k/2$



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VPI Example: Weather

MEU with no evidence

$$MEU(o) = \max_a EU(a) = 70$$

MEU if forecast is bad

$$MEU(F = \text{bad}) = \max_a EU(a|\text{bad}) = 53$$

MEU if forecast is good

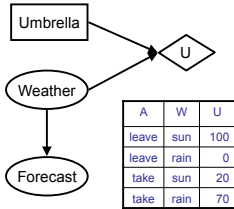
$$MEU(F = \text{good}) = \max_a EU(a|\text{good}) = 95$$

Forecast distribution

F	P(F)
good	0.59
bad	0.41

$$0.59 \cdot (95) + 0.41 \cdot (53) - 70 = 77.8 - 70 = 7.8$$

$$VPI(E|e') = \left(\sum_{e'} P(e'|e) MEU(e, e') \right) - MEU(e)$$



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Value of Information

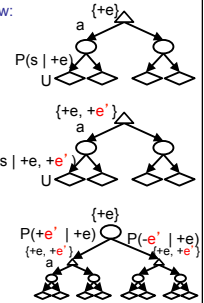
- Assume we have evidence $E=e$. Value if we act now:

$$MEU(e) = \max_a \sum_s P(s|e) U(s, a)$$
- Assume we see that $E' = e'$. Value if we act then:

$$MEU(e, e') = \max_a \sum_s P(s|e, e') U(s, a)$$
- BUT E' is a random variable whose value is unknown, so we don't know what e' will be
- Expected value if E' is revealed and then we act:

$$MEU(e, E') = \sum_{e'} P(e'|e) MEU(e, e')$$
- Value of information: how much MEU goes up by revealing E' first then acting, over acting now:

$$VPI(E'|e) = MEU(e, E') - MEU(e)$$



VPI Properties

- Nonnegative

$$\forall E', e : VPI(E'|e) \geq 0$$

- Nonadditive --- consider, e.g., obtaining E_j twice

$$VPI(E_j, E_k|e) \neq VPI(E_j|e) + VPI(E_k|e)$$

- Order-independent

$$\begin{aligned} VPI(E_j, E_k|e) &= VPI(E_j|e) + VPI(E_k|e, E_j) \\ &= VPI(E_k|e) + VPI(E_j|e, E_k) \end{aligned}$$

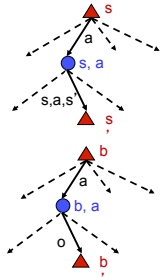
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Quick VPI Questions

- The soup of the day is either clam chowder or split pea, but you wouldn't order either one. What's the value of knowing which it is?
- There are two kinds of plastic forks at a picnic. One kind is slightly sturdier. What's the value of knowing which?
- You're playing the lottery. The prize will be \$0 or \$100. You can play any number between 1 and 100 (chance of winning is 1%). What is the value of knowing the winning number?

POMDPs

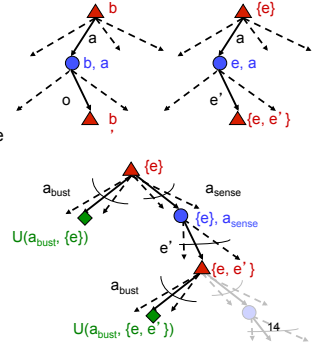
- MDPs have:
 - States S
 - Actions A
 - Transition fn $P(s' | s, a)$ (or $T(s, a, s')$)
 - Rewards $R(s, a, s')$
- POMDPs add:
 - Observations O
 - Observation function $P(o | s)$ (or $O(s, o)$)
- POMDPs are MDPs over belief states b (distributions over S)
- We'll be able to say more in a few lectures



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Example: Ghostbusters

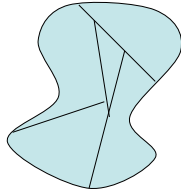
- In (static) Ghostbusters:
 - Belief state determined by evidence to date $\{e\}$
 - Tree really over evidence sets
 - Probabilistic reasoning needed to predict new evidence given past evidence
- Solving POMDPs
 - One way: use truncated expectimax to compute approximate value of actions
 - What if you only considered busting or one sense followed by a bust?
 - You get a VPI-based agent!



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More Generally

- General solutions map belief functions to actions
 - Can divide regions of belief space (set of belief functions) into policy regions (gets complex quickly)
 - Can build approximate policies using discretization methods
 - Can factor belief functions in various ways
- Overall, POMDPs are very (actually PSACE-) hard
- Most real problems are POMDPs, but we can rarely solve them in general!



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